

3.9  
49

$$y = e^x$$

(0, 0)

$$y' = e^x$$

Oct 23-10:10 AM

### Opener

Non-Calculator

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$$\frac{d}{dx}(xe^{\ln x^2}) = x^3$$

(A)  $1+2x$     (B)  $x+x^2$     (C)  $3x^2$     (D)  $x^3$     (E)  $x^2+x^3$

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$$f = x \quad f' = 1$$

$$g = e^{\ln x^2} \quad g' = e^{\ln x^2} \cdot \left(\frac{1}{x^2}\right) \cdot 2x$$

$$e^{\ln x^2} + x e^{\ln x^2} \cdot \frac{2}{x} = 3e^{\ln x^2}$$

Oct 1-8:22 AM

1) True or False. The derivative of  $y = 2^x$  is  $2^x$ . Justify your answer.  
 F  $y' = 2^x \cdot \ln 2$

2) True or False. The derivative of  $y = e^{2x}$  is  $2(\ln 2) e^{2x}$ . Justify your answer.  
 F  $y' = e^{2x} \cdot 2$

3) Which of the following is  $dy/dx$  if  $y = \tan(4x)$ ?

a)  $4 \sec(4x)\tan(4x)$     b)  $\sec(4x)\tan(4x)$     c)  $4 \cot(4x)$   
 d)  $\sec^2(4x)$     (e)  $4 \sec^2(4x)$      $y' = \sec^2(4x) \cdot 4$

Oct 19-10:14 AM

### 3-8 Derivates of the Inverse Trig Funcons

#### Learning Objectives:

I can calculate the derivaves of the inverse trig funcons

I can calculate the derivaves of inverse funcons given informaon about the funcon.

Oct 1-8:22 AM

### Derivates of Inverse Trig Funcons

$$\frac{d}{dx}(\sin^{-1} x) = \frac{1}{\sqrt{1-x^2}} \quad \frac{d}{dx}(\cos^{-1} x) = \frac{-1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx}(\tan^{-1} x) = \frac{1}{1+x^2} \quad \frac{d}{dx}(\cot^{-1} x) = \frac{-1}{1+x^2}$$

$$\frac{d}{dx}(\sec^{-1} x) = \frac{1}{|x|\sqrt{x^2-1}} \quad \frac{d}{dx}(\csc^{-1} x) = \frac{-1}{|x|\sqrt{x^2-1}}$$

Oct 1-8:22 AM

### Ex1. Find the Derivate

1.)  $y = x^2 \sin^{-1} x$   
 $f' \cdot g + f \cdot g'$      $2x \sin^{-1} x + \frac{x^2}{\sqrt{1-x^2}}$

2.)  $y = \frac{\cos^{-1} x}{e^x}$   
 $\frac{f' \cdot g - f \cdot g'}{g^2}$      $\frac{\frac{-1}{\sqrt{1-x^2}}(e^x) - \cos^{-1} x (e^x)}{(e^x)^2}$

Oct 1-8:22 AM

3.)  $y = \sin^{-1}(4x)$

$$y' = \frac{1}{\sqrt{1-(4x)^2}} \cdot 4$$

Oct 1-8:22 AM

4.)  $y = \cos^{-1}\left(\frac{2}{x}\right)$

$$\frac{-2}{x^2} \cdot \frac{-1}{\sqrt{1-(2/x)^2}} = \frac{2}{x^2 \sqrt{1-\frac{4}{x^2}}}$$

$$= \frac{2}{x^2 \sqrt{\frac{x^2-4}{x^2}}} = \frac{2}{x^2 \frac{\sqrt{x^2-4}}{x}} = \frac{2}{x \sqrt{x^2-4}}$$

5.)  $y = \tan^{-1}(x^2 e^x)$

$$\frac{1}{1+(x^2 e^x)^2} (2x e^x + x^2 e^x)$$

Oct 1-8:22 AM

### Inverse Funcons

$y = f(x)$        $y = f^{-1}(x)$

$y = x^3$        $x = y^3$        $y = \sqrt[3]{x}$

$y' = 3x^2$   
 $= 3(2)^2$   
 $= 12$

$\frac{1}{3} x^{-2/3}$   
 $= \frac{1}{12}$

Oct 1-8:22 AM

Ex.1 Certain values of the funcon  $f(x)$  and its derivaves  $f'(x)$  are shown in the table below

x	f(x)	f'(x)
1	5	-3
2	1	-7
3	-8	-1/2

a.) Find  $\frac{d}{dx}(f^{-1}(x))$  @  $x=1$   
 $f^{-1}(1, 2) = \frac{-1}{7}$

b.) Find the equaon of the tangent line to  $y = f^{-1}(x)$  @  $x=1$   
 $y - 2 = -\frac{1}{7}(x - 1)$

Oct 1-8:22 AM

### Homework

pg 170 # 1, 3, 24, 27, 28, 29, 35-40

Oct 1-8:22 AM